

1) If $L: V \rightarrow W$ is a linear transformation,

a) and the image of L contains a basis for W ,

then L is onto

b) If $\{v_i\}_{i=1}^k$ is a basis for V , and the set

$\{L(v_i)\}_{i=1}^k$ is linearly independent, show L is 1-1.

2) Let ~~T~~ $L: \mathbb{R}^4 \rightarrow \mathbb{R}^4$ be the linear transformation defined by $L(e_i) = e_i + e_i$.

Show L is an isomorphism, and compute the matrix for L with respect to the usual basis of \mathbb{R}^4 .

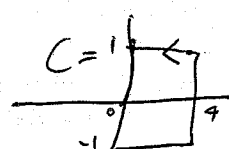
3) Use the formula

$$\left(\sum_{n=0}^{\infty} a_n z^n\right) \left(\sum_{n=0}^{\infty} b_n z^n\right) = \left(\sum_{n=0}^{\infty} \left(\sum_{k=0}^n a_k b_{n-k}\right) z^n\right)$$

to compute the ~~the Taylor series for~~

first 4 terms of the Taylor series for $\sin z \cos z$.

4) Find the solutions of $z^6 = i$, and of $z^5 = 16\sqrt{2}(1+i)$
Can Draw them!

5) Compute $\int_C \frac{z}{(z-2)(z+2)} dz$ where $C =$ 

6) State Cauchy's theorem. Explain how Cauchy's theorem lets you prove the residue theorem for functions with isolated singularities.

7) Prove $\int_C f(z) dz = 2\pi i b_1$, when C is a small contour around z_0 , and b_1 is the coefficient of z^{-1} in a Laurent series at z_0 .